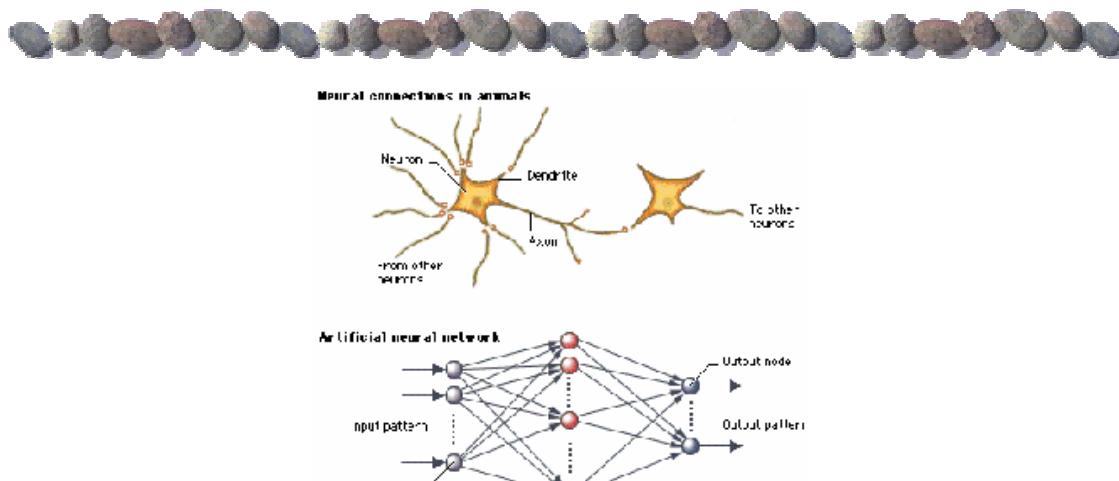


# Programming in MATLAB

## Chapter 2: Artificial Neural Network (Perceptron)

Gp.Capt.Thanapant Raicharoen, PhD



# Outline

- **Introduction to Artificial Neural Network**
- **Machine Learning and Learning Rule**
- **Perceptron Learning Rule**
- **Perceptron program in MATLAB**
- **Perceptron MATLAB Toolbox**

# Human vs. Computer

## ■ Speed

- Human: Neuron Cell Signal 1000 times/Second
- Computer: CPU 1 GHz

## ■ (mathematical) Processing

- Human: not good
- Computer: > 1000 MFLOP

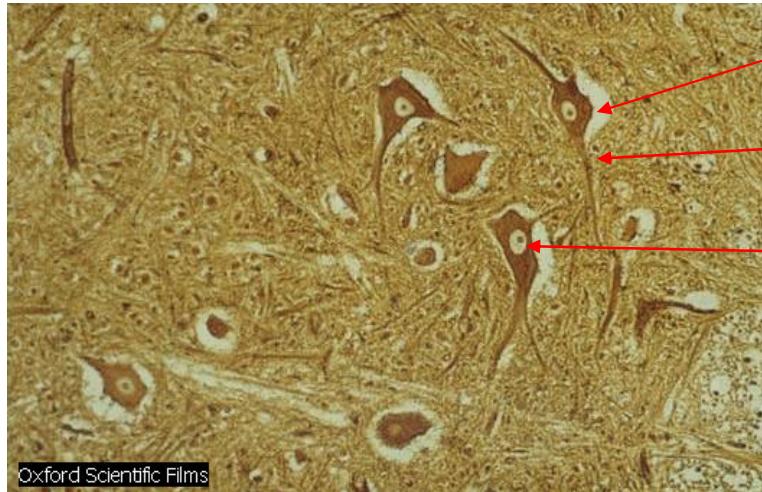
## ■ Problem Analysis

- Human: good
- Computer: not good

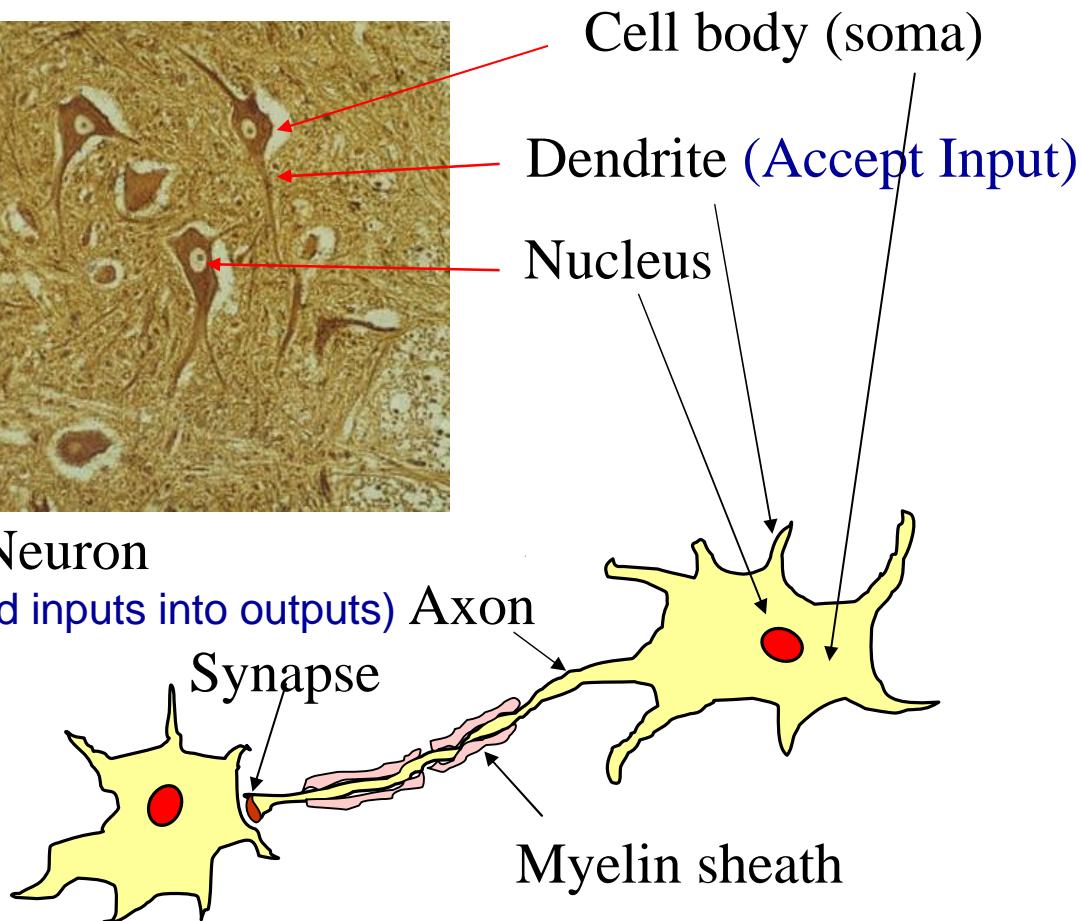
## ■ (pattern) Recognition

- Human: good
- Computer: not good

# Human Brain



Neuron  
(Turn the processed inputs into outputs)



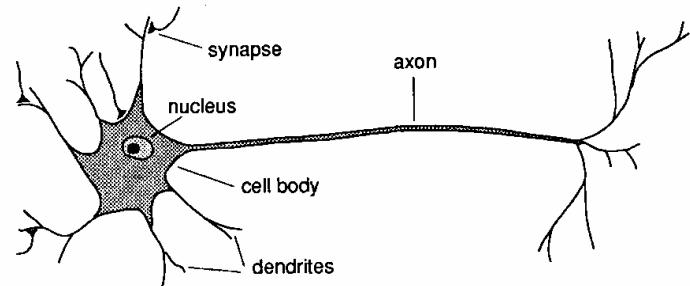
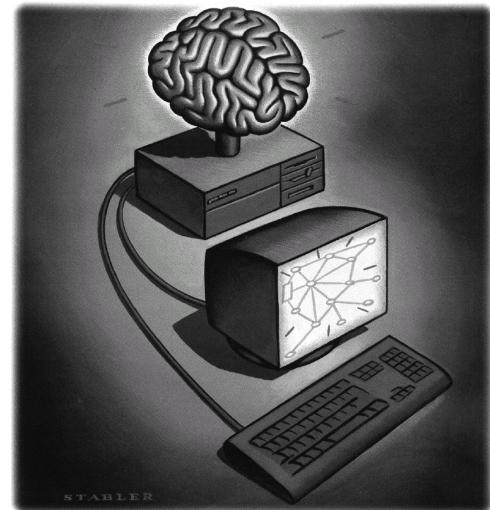
# (Artificial) Neural Networks

## ■ What is a Neural Network?

- Biologically motivated approach to machine learning
- Similarity with biological network

## ■ Human brain

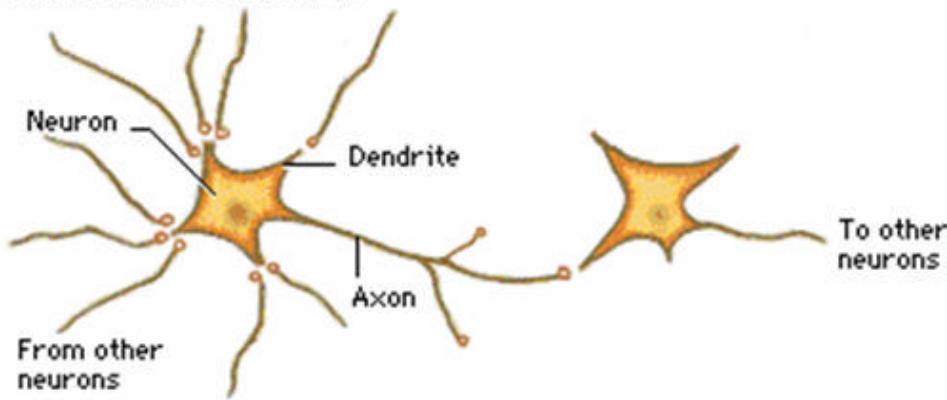
- interconnected network of  $10^{11}$  neurones (100,000,000,000)
- each connected to  $10^4$  others
- surprisingly complex decisions, surprisingly quickly ( $10^{-1}$ s)
- robust & fault tolerant, flexible
- deals with fuzzy, noisy, or inconsistent information



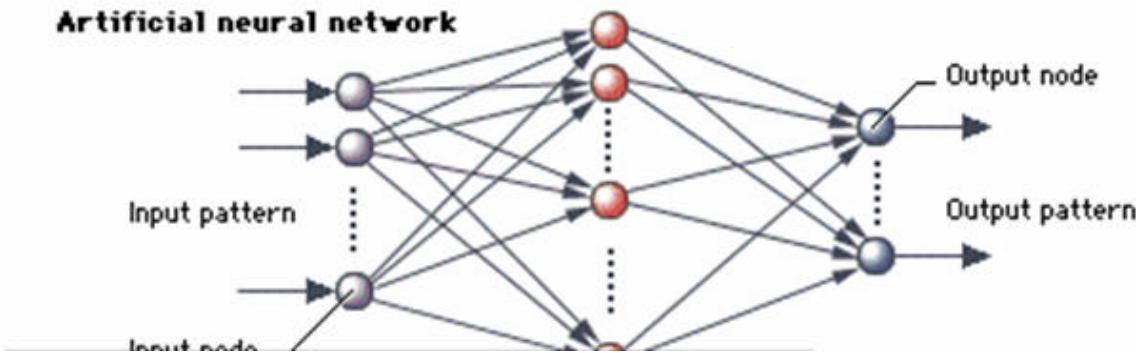
# (Artificial) Neural Networks

A biological neurone showing its cell body and connections

**Neural connections in animals**



**Artificial neural network**



A non-linear model for a neurone

# Biological and Artificial Neural Network

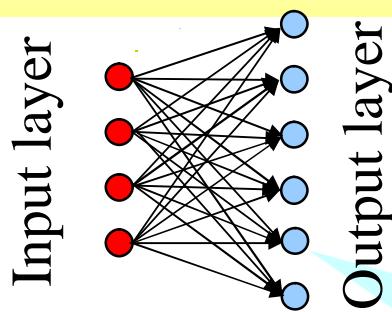
## ■ Biological NN

- Cell Body
- Dendrite
- Soma
- Axon

## ■ Artificial NN

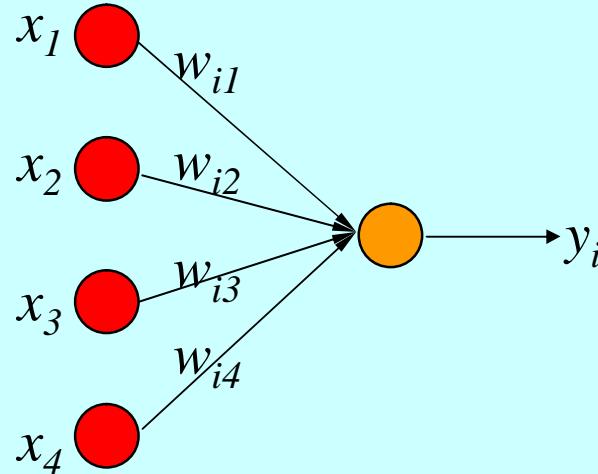
- Neurons
- Weights or interconnections
- Net Input
- Output

# A Single Layer Perceptron Network



For each node, the output is given by

$$y_i = g\left(\sum_{j=1}^N w_{ij}x_j - \mathbf{m}_i\right)$$



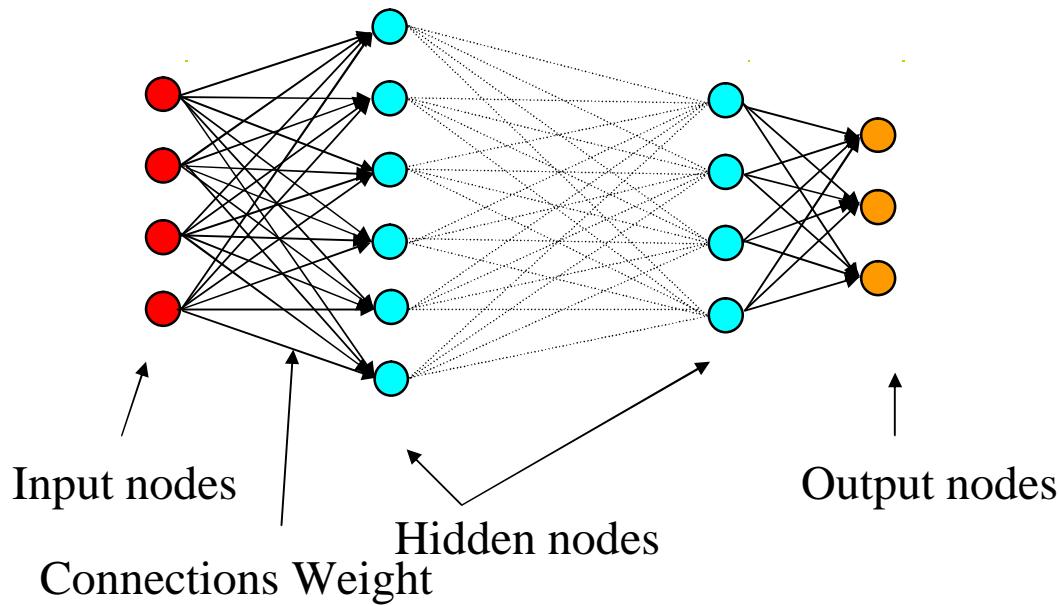
$w_{ij}$  = Connection *weight* of branch  $(i,j)$

$x_j$  = *Input data* from node  $j$  in the input layer

$\mathbf{m}_i$  = *Bias* or *Threshold* value of node  $i$  in the output layer

$g$  = *Activation* or *Transfer function*

# (Artificial) Neural Network



Output of each node (mathematical equation)

$$\begin{aligned}y_i &= f(w_i^1 x_1 + w_i^2 x_2 + w_i^3 x_3 + \cdots + w_i^m x_m) \\&= f\left(\sum_j w_i^j x_j\right)\end{aligned}$$

$X_i$  = input from the other nodes

$w_i^j$  = weight of each connection

# Mathematic Foundation for Neural Network

- **Linear Algebra** is the core of the mathematics required for understanding neural network

- Vectors and Vector Spaces
- Inner Product, Norm and Orthogonality
- Matrices, Linear Transformations
- Eigenvalues and Eigenvectors
- Etc.

- **Calculus**

- Differentiation and Integration

- **Probability**

- **Set Theory**

# Machine Learning

- Machine learning is programming computers to optimize a performance criterion using **example data or past experience**.
- We need learning in cases where we cannot directly write a computer program to solve a given problem.
- Learning is used when:
  - Human expertise does not exist (navigating on Mars),
  - Humans are unable to explain their expertise (speech recognition)
  - Solution changes in time (routing on a computer network)
  - Solution needs to be adapted to particular cases (user biometrics)

# Three Types of Learning

## ■ Supervised Learning

- Learning (Training) with teacher (Supervisor)
- There exist input (training) data and right output (response) target.

## ■ Unsupervised Learning

- Learning (Training) without teacher (Supervisor)
- There exist input (training) data without right output (response) target.

## ■ Reinforcement Learning

- Learning (Training) assumed with teacher (Supervisor)
- There exist input (training) data and output (response) target (but do not know right or not).

# Neural Network Model

## ■ Supervised Learning

- Perceptron
- Multi-Layer Perceptron (MLP)
  - Feed Forward Network
  - Back Propagation
- Radius Bias Function (RBF)
- Support Vector Machine (SVM)
- k-Nearest Neighbour (k-NN)
- etc.

## ■ Unsupervised Learning

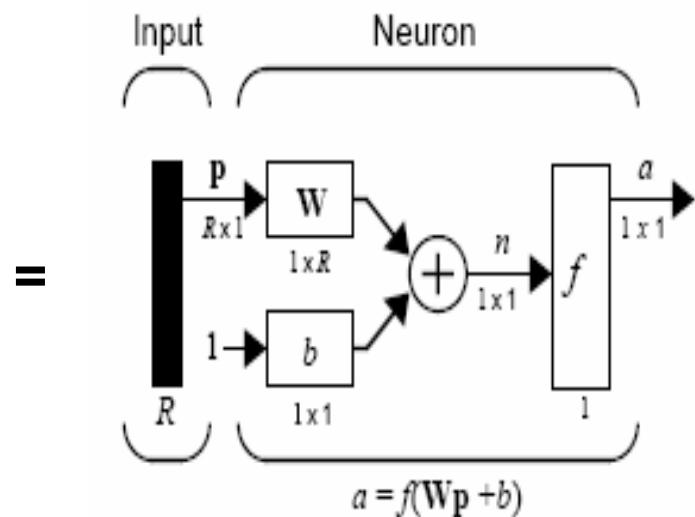
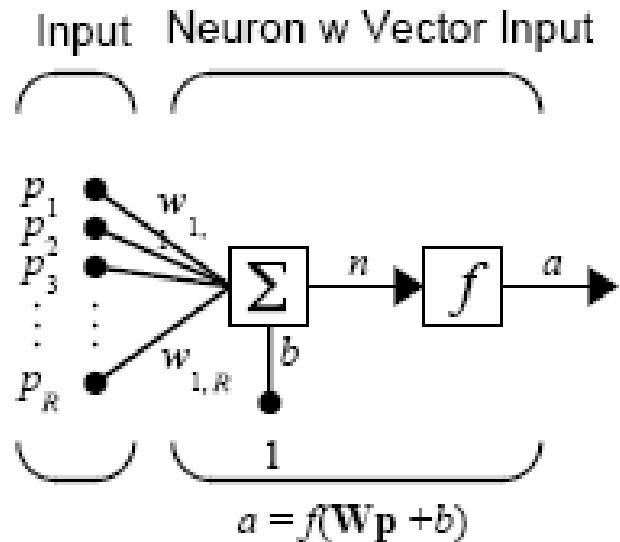
- Clustering
- Self Organisation Map (SOM)
- Principal Component Analysis (PCA)
- etc.

## ■ Reinforcement Learning

# **Neural Network Applications**

- Pattern Recognition
- Process identification & control
- Time series prediction
- Forecasting/Market Prediction: finance and banking
- Data Mining and Intelligent Data Analysis
- Medicine: analysis of electrocardiogram data, RNA & DNA sequencing, drug development without animal testing
- Control: process, robotics
- Manufacturing: quality control, fault diagnosis
- etc.

# Neuron Model (One Neuron) by MATLAB

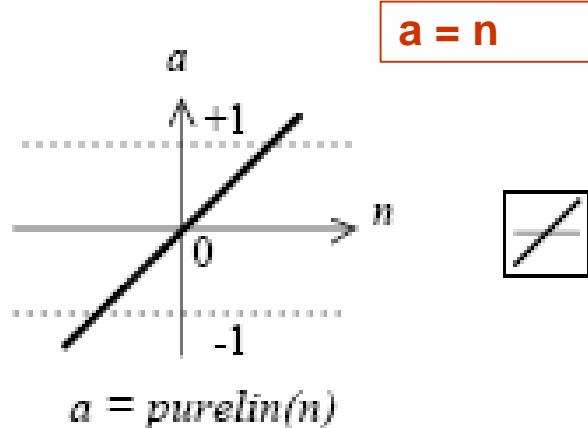


- $p_1, p_2, \dots, p_R$  = inputs (vector)
- $w_1, w_2, \dots, w_R$  = synaptic weights
- $b$  = threshold (Bias)
- $f$  = activation (transfer) function:
- $a$  = output:  $a = f(\mathbf{W}\mathbf{p} + b) = f(n)$

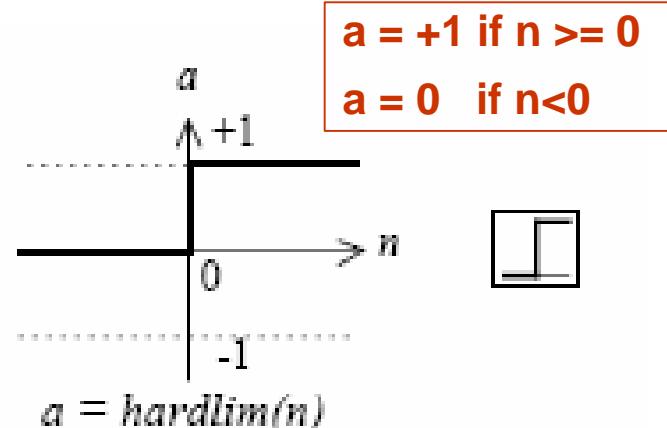
$$n = w_{1,1}p_1 + w_{1,2}p_2 + \dots + w_{1,R}p_R + b$$

$$\mathbf{n} = \mathbf{W} * \mathbf{p} + \mathbf{b}$$

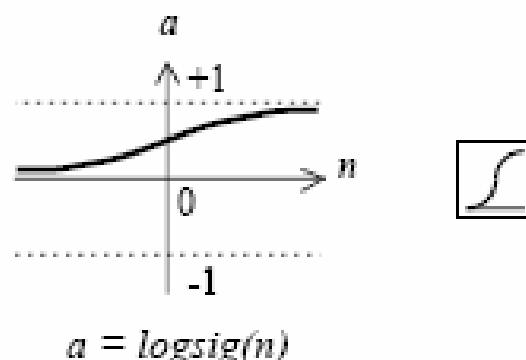
# activation (transfer) functions



Linear Transfer Function

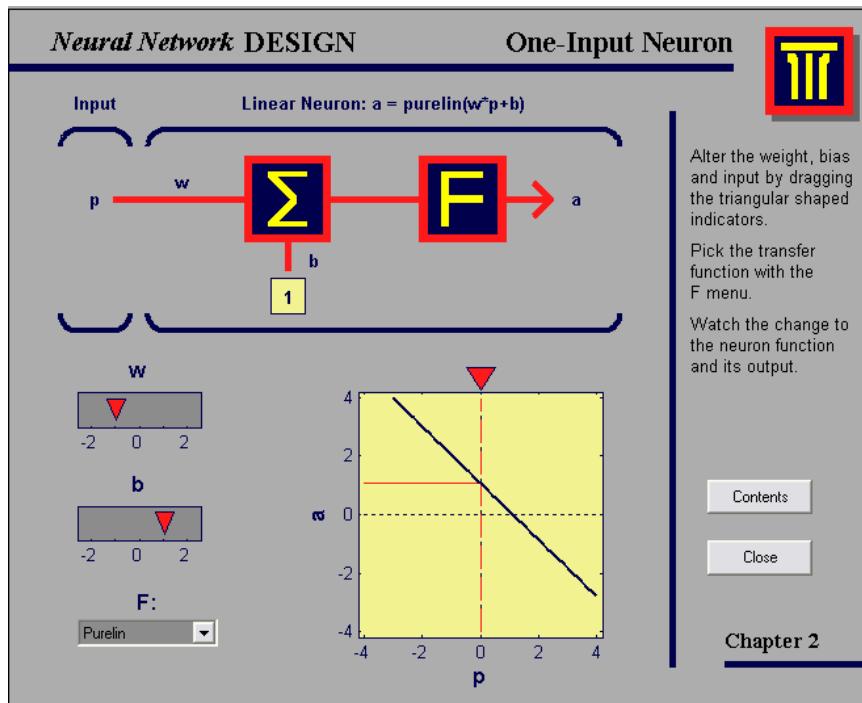


Hard-Limit Transfer Function



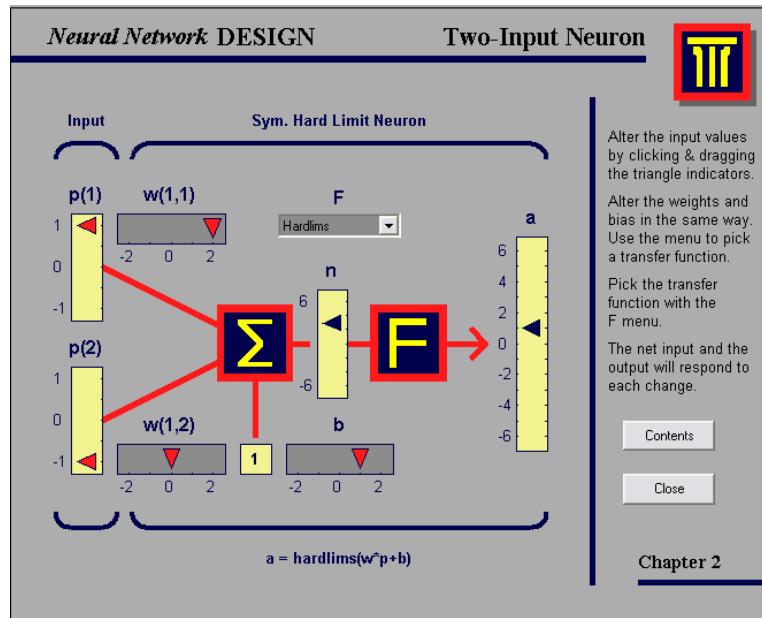
Log-Sigmoid Transfer Function

# Neuron Model in MATLAB (Single/One-Input)



- $p_1$  – inputs (patterns) = 0
- $w_1$  - synaptic weights = -1
- $b$  - threshold (Bias) = 1
- $f$  - activation (transfer) function: = pureline
- $a$  - output: = 1

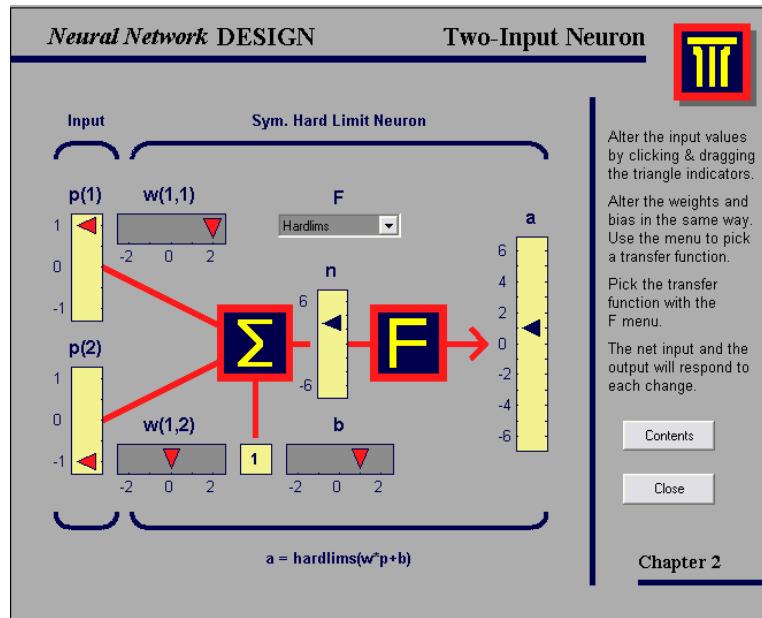
# Neuron Model in MATLAB (Two-Input)



- $p_1, p_2$  - inputs (patterns) =  $(1, -1)$
- $w_1, w_2$  - synaptic weights =  $(2, 0)$
- $b$  - threshold (Bias) = 1
- $f$  - activation (transfer) function:  
= Hard Limit
- $a$  - output: = 1

```
% ex_One_Neural.m
p = [1; -1]; % R = 2
W = [2 0];
b = 1;
n = W*p + b;
a = hardlim(n);
```

# Neuron Model in MATLAB (Two-Input)



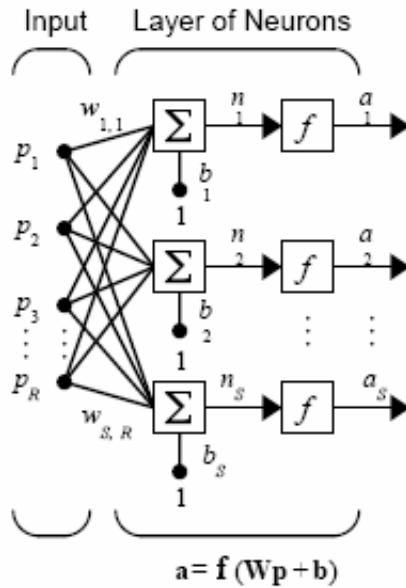
- $p_1, p_2$  - inputs (patterns) =  $(1, -1)$
- $w_1, w_2$  - synaptic weights =  $(2, 0)$
- $b$  - threshold (Bias) = 1
- $f$  - activation (transfer) function:  
= Sigmoid
- $a$  - output: = 0.9526

```
% ex_One_Neural.m
p = [1; -1]; % R = 2
W = [2 0];
b = 1;
n = W*p + b;
a2 = sigmoid(n);
```

# Neuron Model (S Neuron)

## A Layer of Neurons

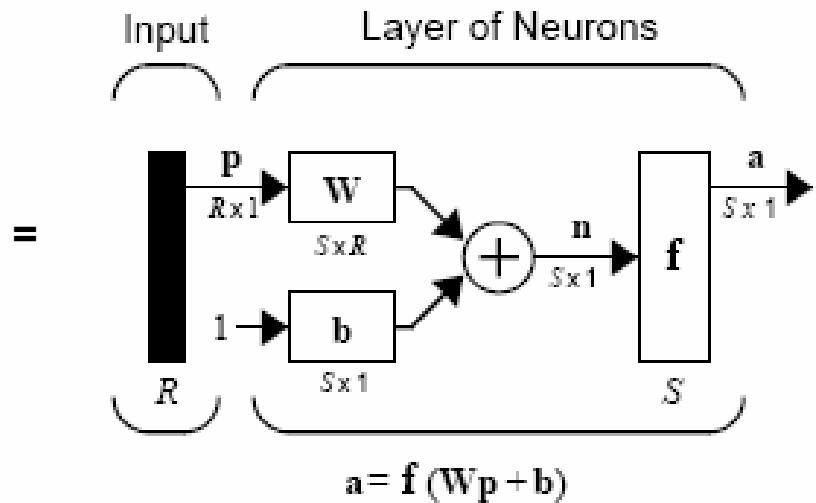
A one-layer network with  $R$  input elements and  $S$  neurons follows.



Where...

$R$  = number of elements in input vector

$S$  = number of neurons in layer



$$n = w_{1,1}p_1 + w_{1,2}p_2 + \dots + w_{1,R}p_R + b$$

$$W = \begin{bmatrix} w_{1,1} & w_{1,2} & \dots & w_{1,R} \\ w_{2,1} & w_{2,2} & \dots & w_{2,R} \\ \vdots & \vdots & \ddots & \vdots \\ w_{S,1} & w_{S,2} & \dots & w_{S,R} \end{bmatrix}$$

% ex\_S\_Neural.m

```
p = [1; -1];
W = [2 0; 1 2; 1 3];
b = [1; 2; 3];
n = W*p + b;
a = hardlim(n);
a2 = sigmoid(n);
```

# Multiple layer of Neuron

```
% ex_Multilayer_Neural2.m
```

```
% Input vector % R = 2 (Column)
```

```
p = [1; -1];
```

```
% Weight & bias for Layer1, 2, 3
```

```
W1 = [2 0; 1 2; 1 3]; % Layer1: S=3 Nodes
```

```
b1 = [1; 2; 3];
```

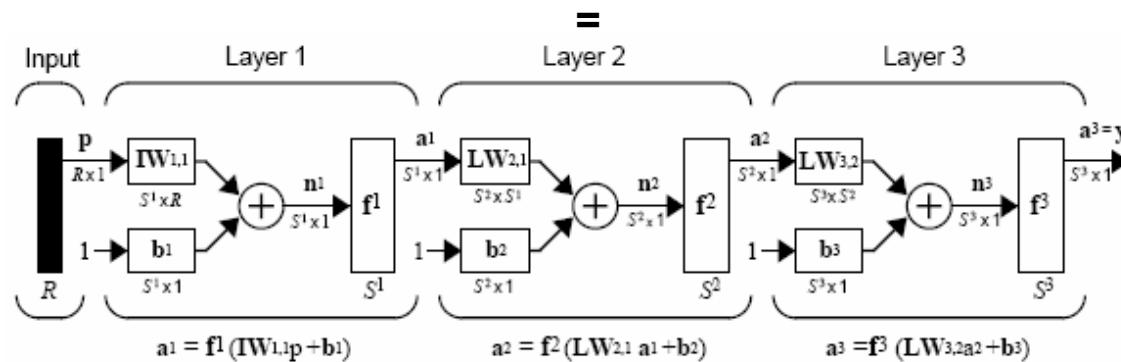
```
W2 = [2 0 1; 1 2 1]; % Layer2: S=2 Nodes
```

```
b2 = [0; 0];
```

```
W3 = [2 0]; % Layer3: S=1 Node
```

```
b3 = [1];
```

```
a3 = sigmoid(W3*(sigmoid(W2*(sigmoid(W1*p+b1))'+b2))'+b3)
```



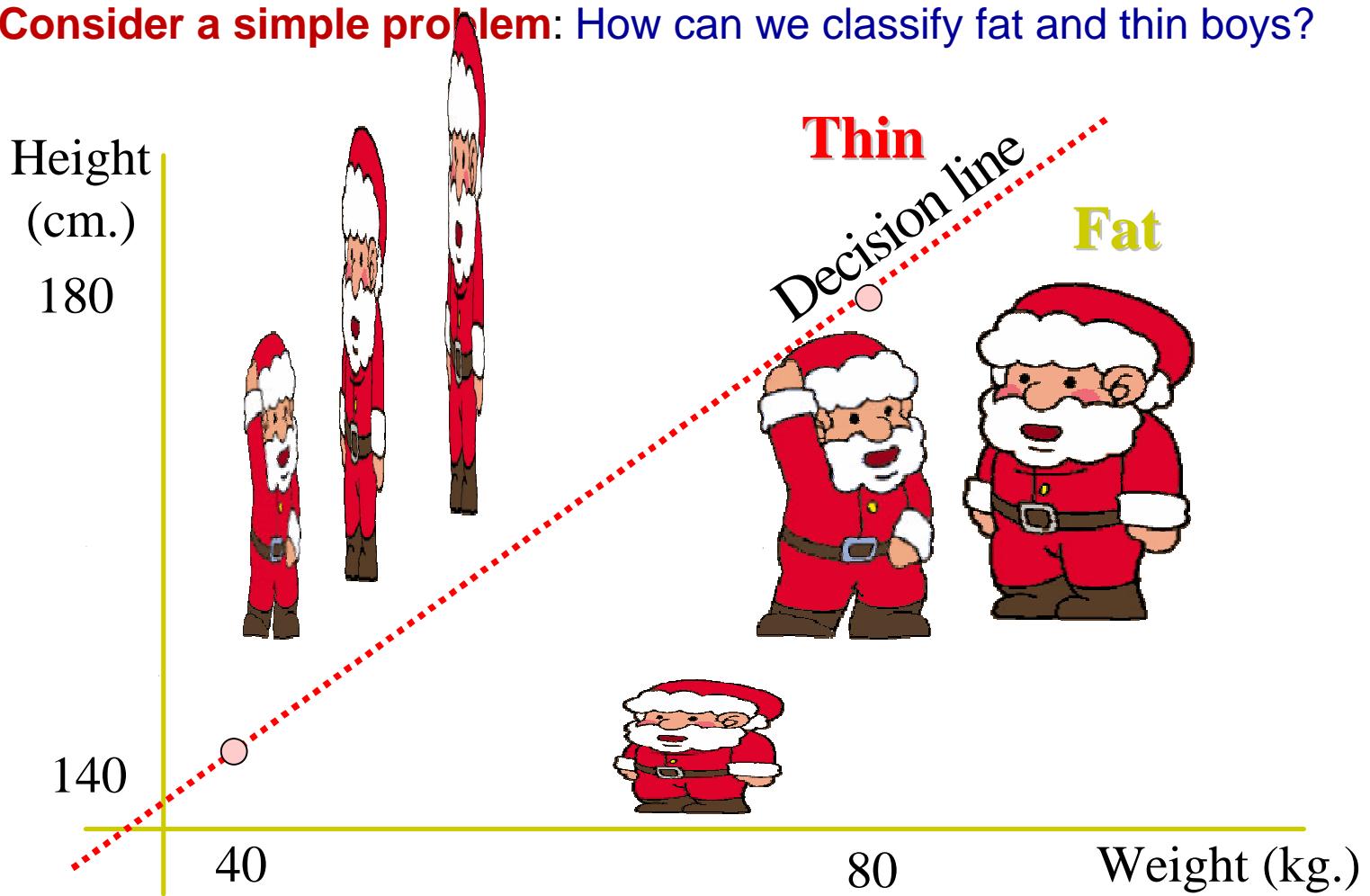
# Programming in MATLAB Exercise

## ■ Exercise:

1. Write MATLAB to solve the question 8 in Exercise 1.
2. Write MATLAB to solve the question 3 in Exercise 2.

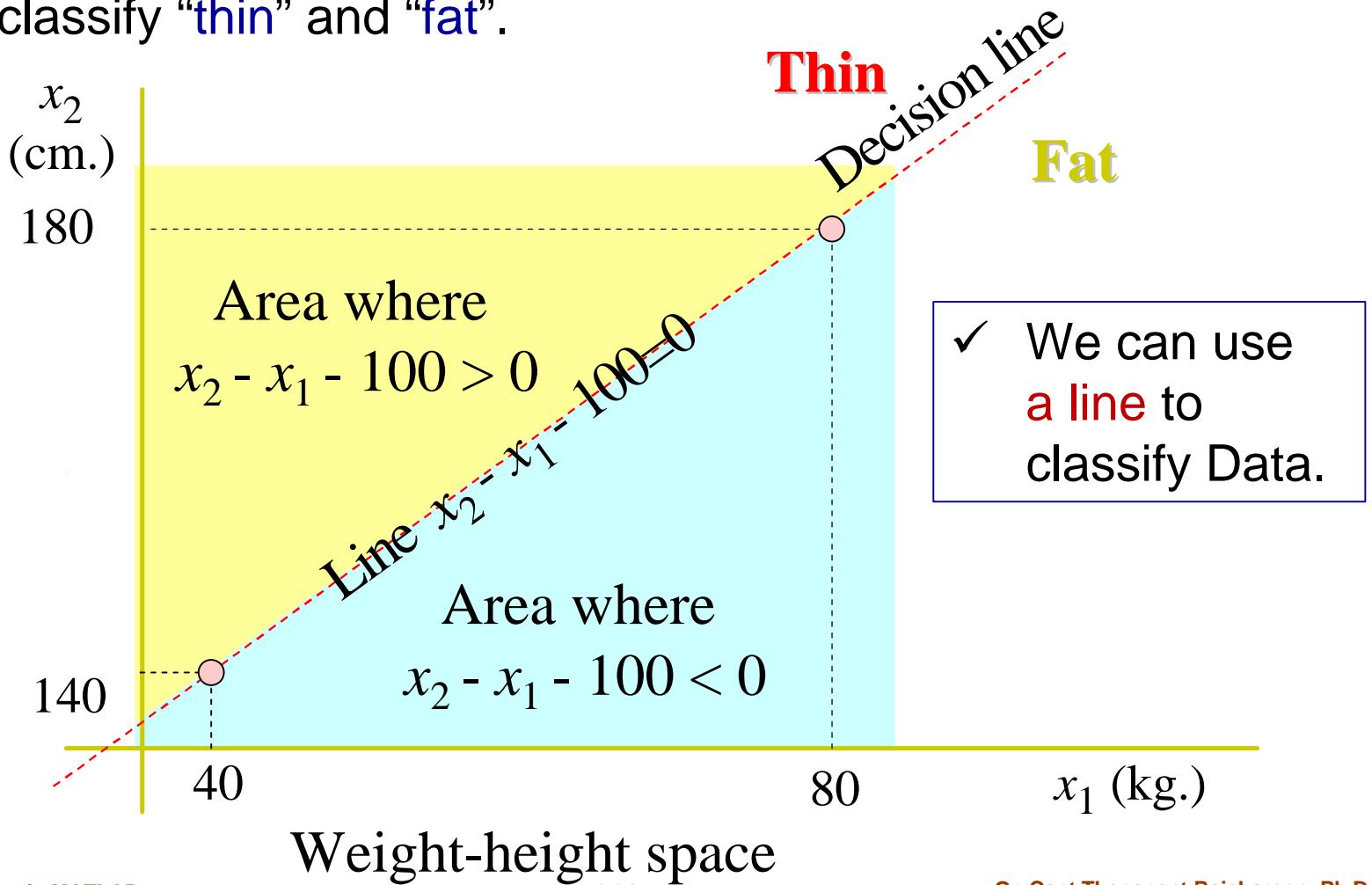
# How can we use a mathematical function to classify ?

- Consider a simple problem: How can we classify fat and thin boys?



# How can we use a mathematical function to classify ?

- We used 2 inputs, weight ( $x_1$ ) and height ( $x_2$ ), to classify “thin” and “fat”.



# How can we use a mathematical function to classify ?

- We can write the decision function for classifying “thin” and “fat” as follows:

$$y = \begin{cases} 1 \text{ (thin)} & \text{if } x_2 - x_1 - 100 \geq 0 \\ 0 \text{ (fat)} & \text{if } x_2 - x_1 - 100 < 0 \end{cases}$$

or

$$\begin{aligned} y &= g(w_1x_1 + w_2x_2 - m) \\ &= g(-x_1 + x_2 - 100) \end{aligned}$$

where

$$g(z) = \begin{cases} 1 & \text{if } z \geq 0 \\ 0 & \text{otherwise.} \end{cases}$$

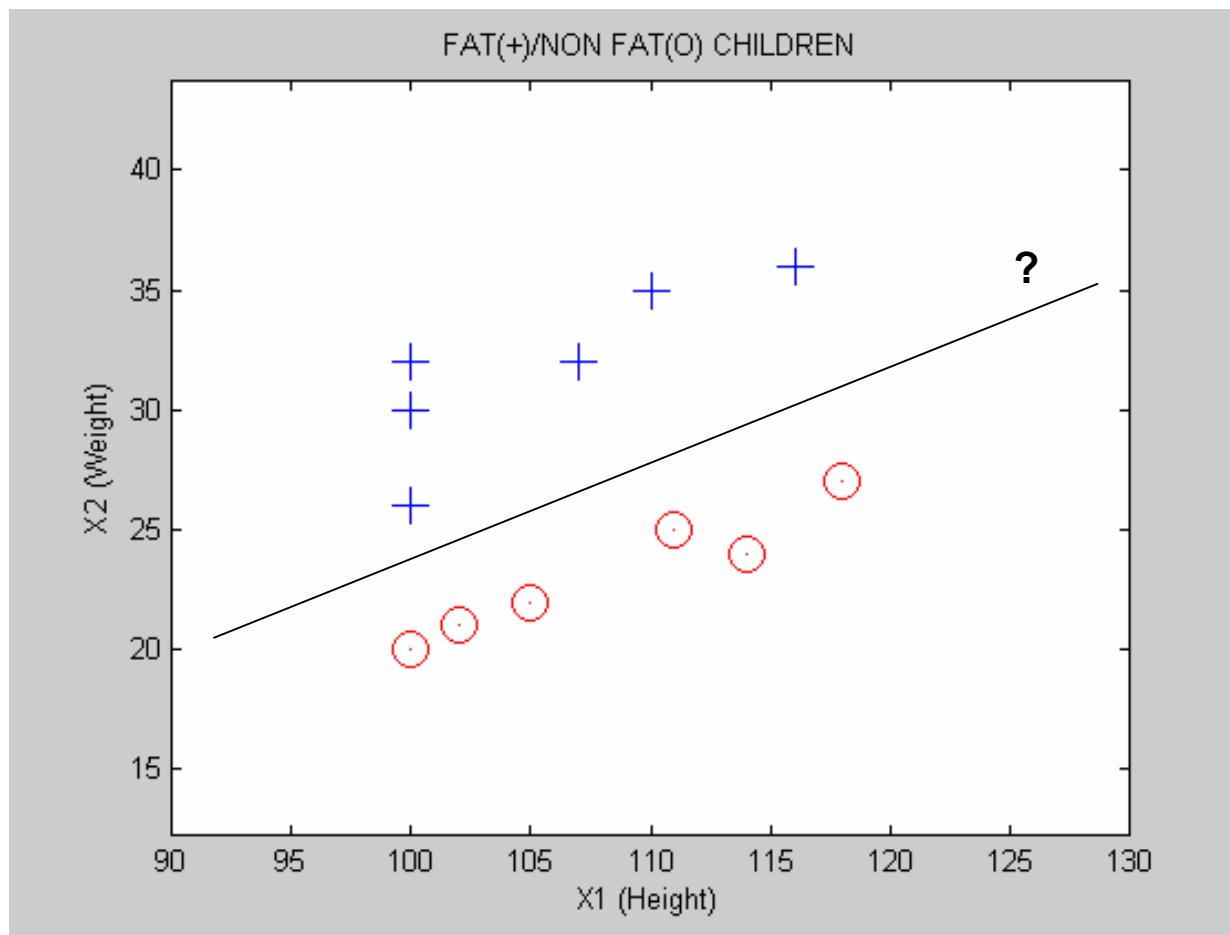
**Advantage:** Universal linear classifier

**Problem:** For a particular problem, **how can we choose suitable weights  $w$  and bias  $\mu$  of the function ?**

# Fat Children Training Samples

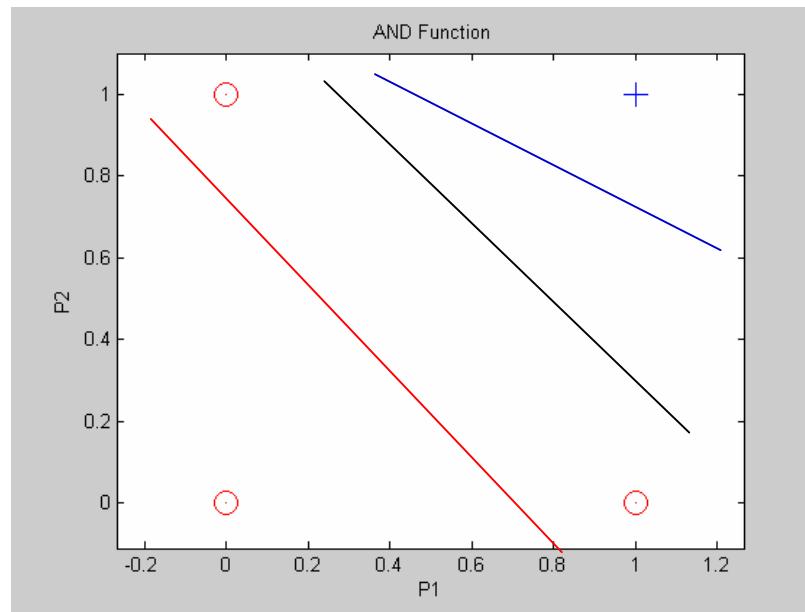
No.	Height (Cm.)	Weight (Kg.)	Fat/Not Fat (+1/-1)
1.	100	20	-1
2.	100	26	+1
3.	100	30	+1
4.	100	32	+1
5.	102	21	-1
6.	105	22	-1
7.	107	32	+1
8.	110	35	+1
9.	111	25	-1
10.	114	24	-1
11.	116	36	+1
12.	118	27	-1

# Fat Children Training Samples



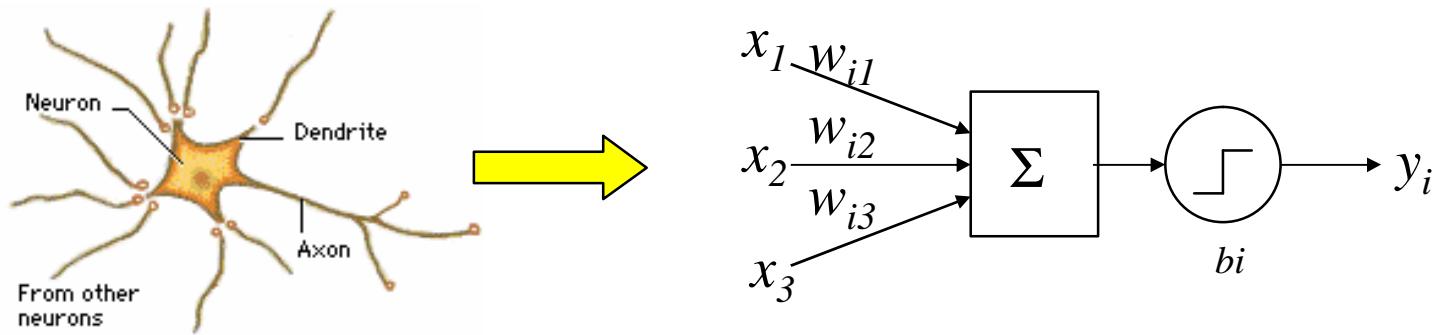
# AND Function

No.	P1	P2	Output/Target
1.	0	0	0
2.	0	1	0
3.	1	0	0
4.	1	1	1



# Supervised Learning: Perceptron Networks

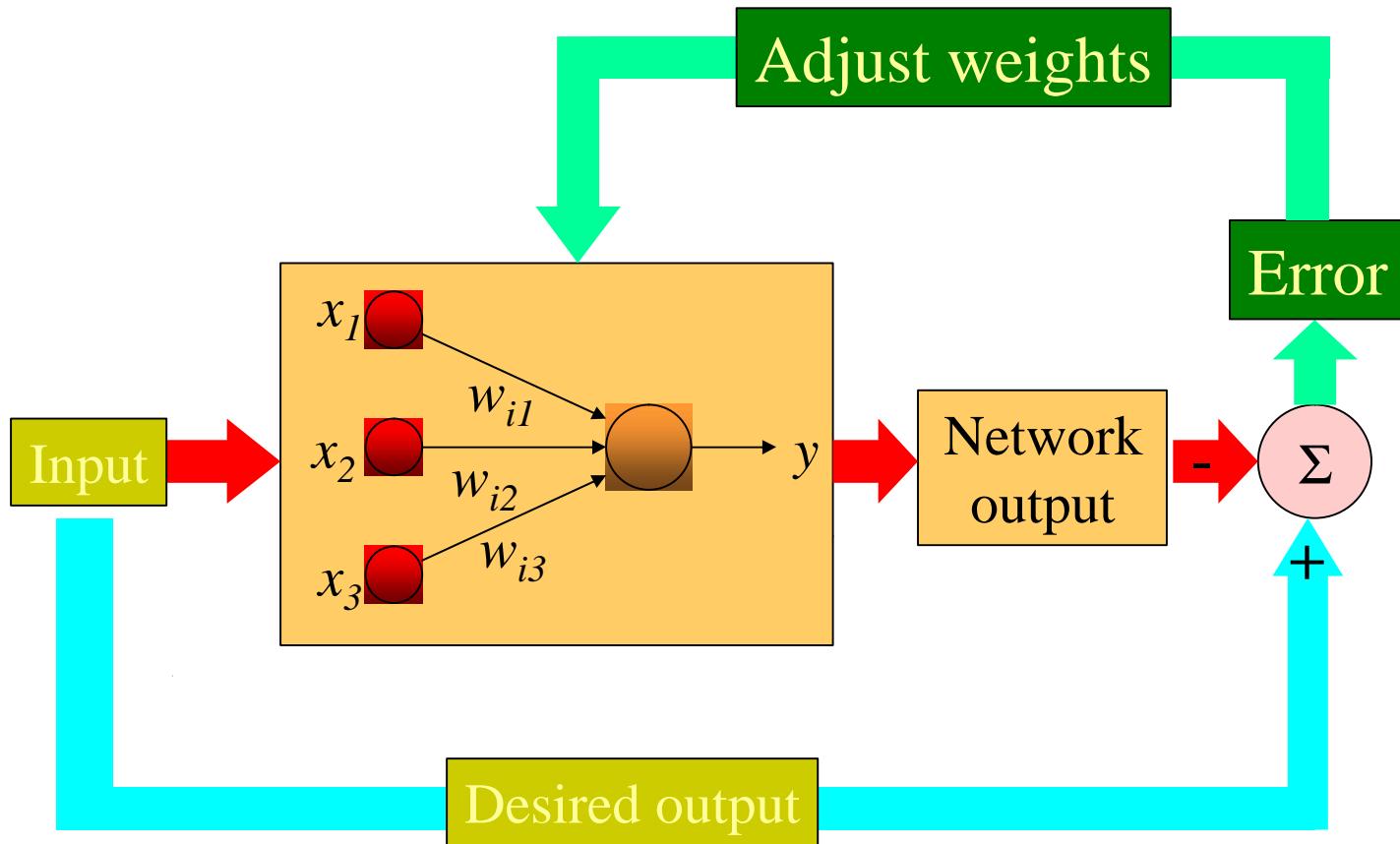
- Rosenblatt and his colleague proposed the Perceptron model in 1962 by inspiration of neural model from McCulloch-Pitts in 1943.



McCulloch-Pitts model

$$\begin{aligned}y_i &= f(w_{i1}x_1 + w_{i2}x_2 + w_{i3}x_3 - b_i) \\&= f\left(\sum_j w_{ij}x_j - b_i\right)\end{aligned}$$

# Learning Algorithm: Training Perceptron Networks



# Perceptron Learning Rule

The perceptron learning rule can be written more succinctly in terms of the error  $e = t - a$ , and the change to be made to the weight vector  $\Delta w$ :

CASE 1. If  $e = 0$ , then make a change  $\Delta w$  equal to 0.

CASE 2. If  $e = 1$ , then make a change  $\Delta w$  equal to  $p^T$ .

CASE 3. If  $e = -1$ , then make a change  $\Delta w$  equal to  $-p^T$ .

All three cases can then be written with a single expression:

$$\Delta w = (t - a)p^T = e p^T$$

The Perceptron Learning Rule can be summarized as follows

$$W^{new} = W^{old} + e p^T \text{ and}$$

$$b^{new} = b^{old} + e$$

where  $e = t - a$ .

# Perceptron Learning Rule

The Perceptron Learning Rule can be summarized as follows

$$\mathbf{W}^{new} = \mathbf{W}^{old} + \mathbf{e} \mathbf{p}^T \text{ and}$$

$$\mathbf{b}^{new} = \mathbf{b}^{old} + \mathbf{e}$$

where  $\mathbf{e} = \mathbf{t} - \mathbf{a}$ .

```
function [ W_new, b_new ] = perceptron(P,t,W,b)
% Perceptron.m (P,t,W,b);
% P = Input vector, t = target, W = Weight, b = bias
% Use Hard limit as Activation Function
a = hardlim(W'*P'+b);
% e = error and Perceptron Rule as follow
e = t-a;
W_new = W + e.*P;
b_new = b + e;
end
```

# Perceptron Training Algorithm

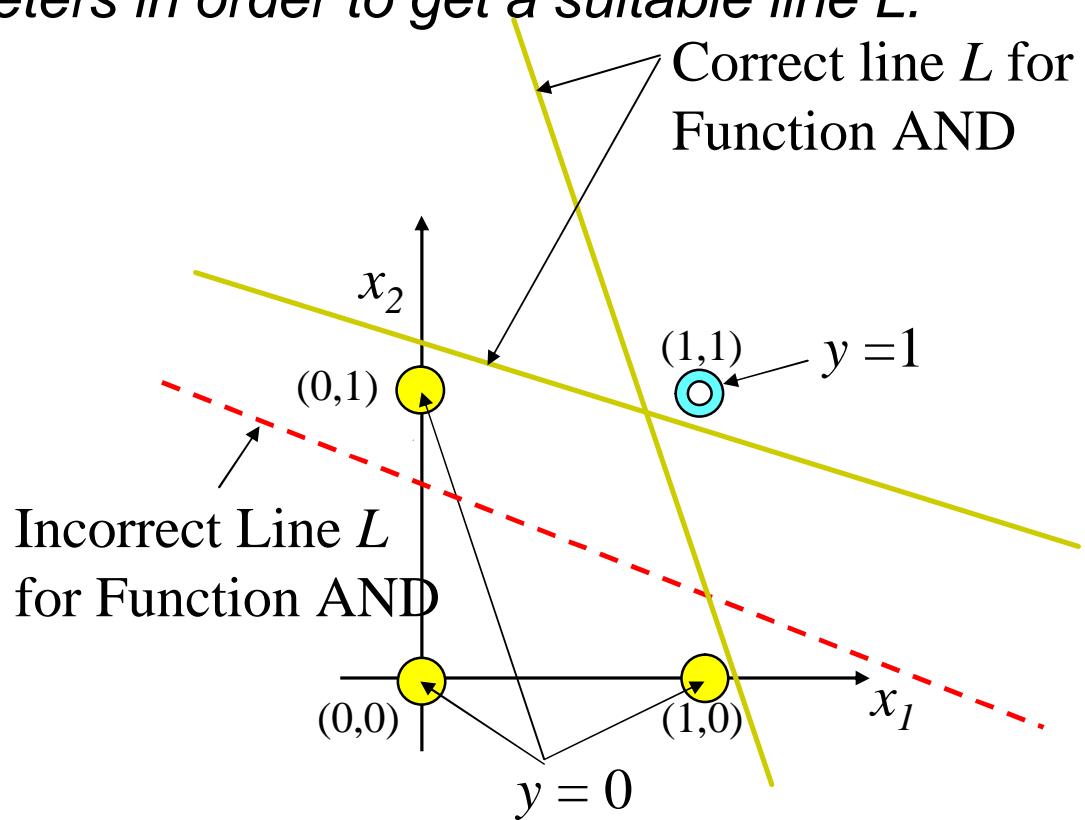
- **Step 1:** Initial weights and bias (can be zero or any).
- **Step 2:** For each training data (input and target) to be classified do **Steps 3-4**.
- **Step 3:** Calculate the response of output unit.
- **Step 4:** The weights and bias are updated by using this learning rule.
- **Step 5:** Test for stopping condition.  
may be the number of loops/iterations (**epoch**).

# How a single layer perceptron works (cont.)

The Slope and Position of the line  $L : w_1x_1 + w_2x_2 - b = 0$  depend on parameters  $w_1$ ,  $w_2$ , and  $b$ . Therefore we have to adjust these parameters in order to get a suitable line  $L$ .

Function AND

$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1



# How a single layer perceptron works (cont.)

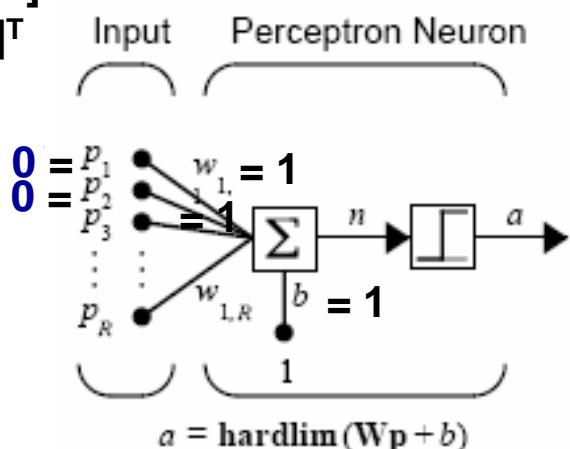
## □ Example: AND Function

```
% Run_AND_Perceptron.m
P = [0 0 1 1; 0 1 0 1]; % AND Function
T = [0 0 0 1];
plotpv(P,T,[-1, 2, -1, 2]); % plot data
% initial weight vector and bias
W = [1 1]; b = 1;
plotpc(W,b); % plot line
epoch = 1; % number of epoch
for j=1:epoch
    for i=1:size(P,2)
        p = P(:,i);
        t = T(i);
        [W b] = perceptron(p',t,W,b);
        plotpc(W,b);
    end
end
% test data test = [0 0]'
test = [0 0];
output = hardlim(W'*test'+b)
```

# AND Function

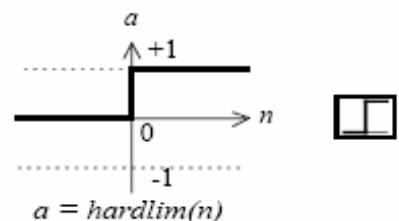
No.	P1	P2	Target	Output (n)	Actual (a)	W1	W2	b
						1	1	1
1.	0	0	0					
2.	0	1	0					
3.	1	0	0					
4.	1	1	1					

$$\mathbf{P} = [\mathbf{P}_1 \quad \mathbf{P}_2]^T \\ = [0 \quad 0]^T$$



Where...

$R$  = number of elements in input vector



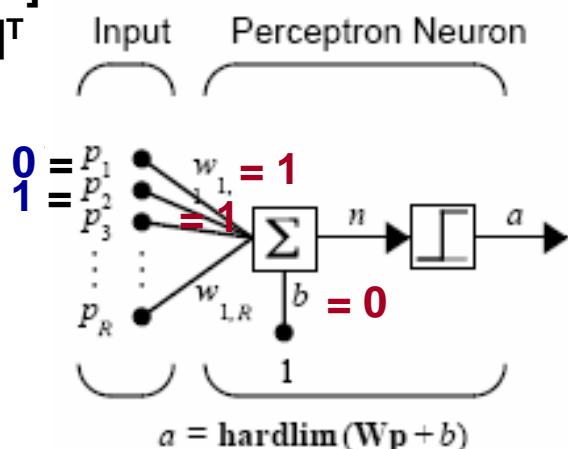
Hard-Limit Transfer Function

# AND Function

No.	P1	P2	Target	Output (n)	Actual (a)	W1	W2	b
						1	1	1
1.	0	0	0	1	1	1	1	0
2.	0	1	0					
3.	1	0	0					
4.	1	1	1					

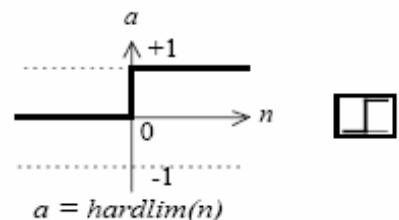
$$P = [P1 \ P2]^T$$

$$= [0 \ 1]^T$$



Where...

R = number of elements in input vector

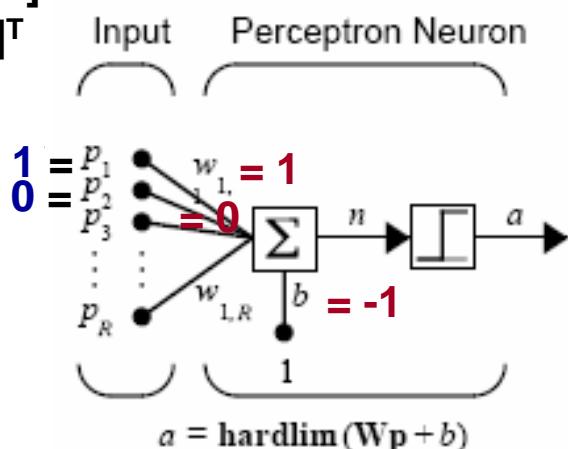


Hard-Limit Transfer Function

# AND Function

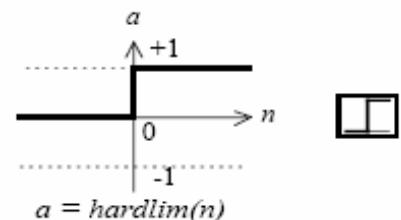
No.	P1	P2	Target	Output (n)	Actual (a)	W1	W2	b
						1	1	1
1.	0	0	0	0	1	1	1	0
2.	0	1	0	1	1	1	0	-1
3.	1	0	0					
4.	1	1	1					

$$\mathbf{P} = [\mathbf{P1} \quad \mathbf{P2}]^T \\ = [1 \quad 0]^T$$



Where...

R = number of elements in input vector



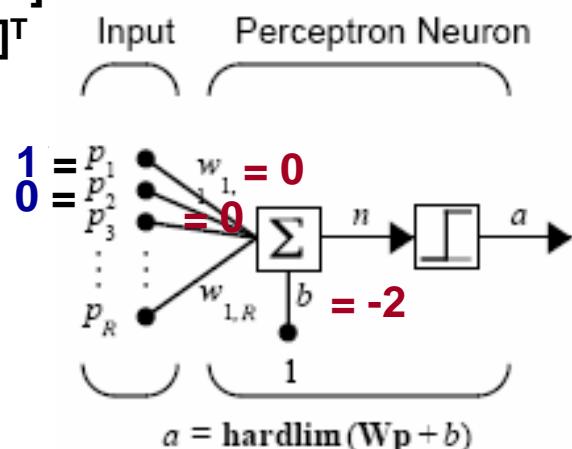
Hard-Limit Transfer Function

# AND Function

No.	P1	P2	Target	Output (n)	Actual (a)	W1	W2	b
						1	1	1
1.	0	0	0	0	1	1	1	0
2.	0	1	0	1	1	1	0	-1
3.	1	0	0	0	1	0	0	-2
4.	1	1	1					

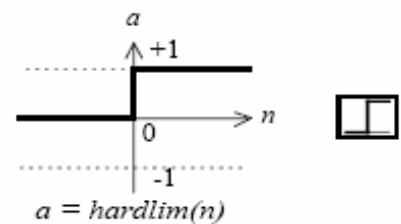
$$P = [P1 \ P2]^T$$

$$= [1 \ 1]^T$$



Where...

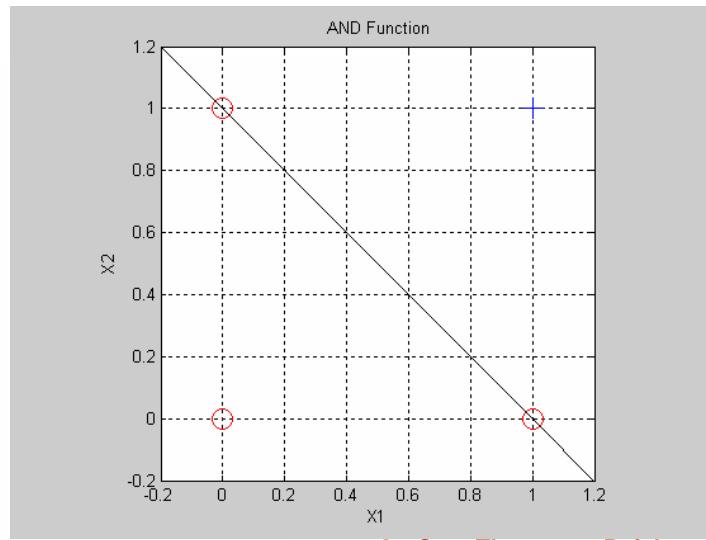
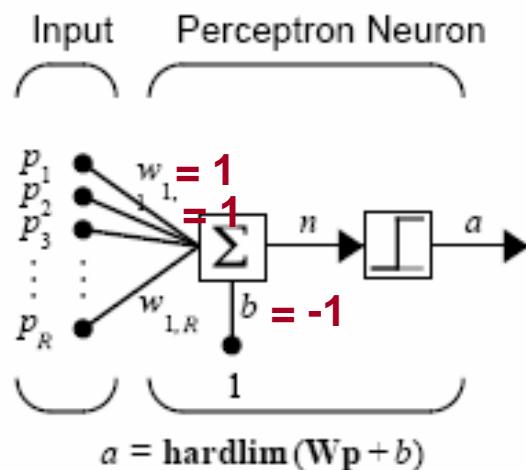
R = number of elements in input vector



Hard-Limit Transfer Function

# AND Function

No.	P1	P2	Target	Output (n)	Actual (a)	W1	W2	b
1.	0	0	0	0	1	1	1	1
2.	0	1	0	1	1	1	0	-1
3.	1	0	0	0	1	0	0	-2
4.	1	1	1	-2	0	1	1	-1

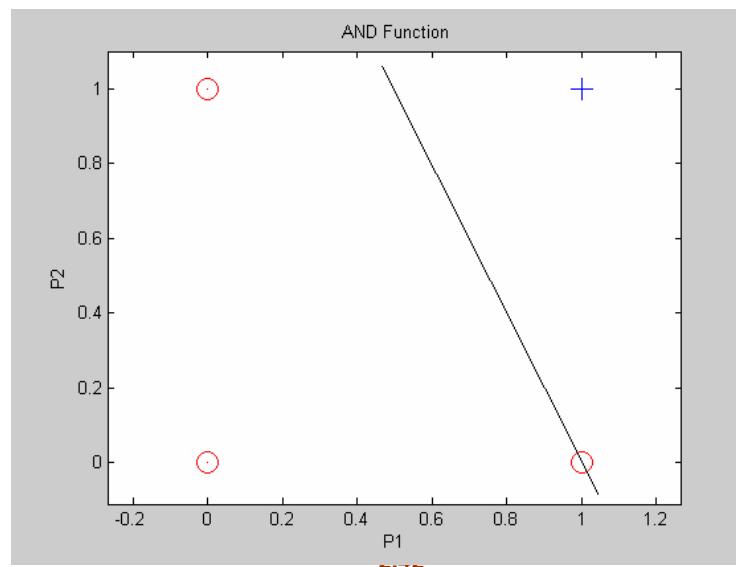


# AND Function

No.	P1	P2	Target	Actual Output	W1	W2	b	
1.	0	0	0	1	1	1	1	1. epoch
2.	0	1	0	1	1	0	-1	
3.	1	0	0	1	0	0	-2	
4.	1	1	1	0	1	1	-1	
No.	P1	P2	Target	Actual Output	W1	W2	b	2. epoch
1.	0	0	0	1	1	1	-1	
2.	0	1	0	1	1	0	-2	
3.	1	0	0	1	1	0	-2	
4.	1	1	1	0	2	1	-1	

# AND Function

No.	P1	P2	Target	Actual Output	W1	W2	b
					2	1	-1
1.	0	0	0	1	2	1	-1
2.	0	1	0	1	2	0	-2
3.	1	0	0	1	1	0	-3
4.	1	1	1	0	2	1	-2



# Learning Algorithm: Training Perceptron Networks (cont.)

Function AND

$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1

epoch: 16  
epoch: 12  
epoch: 8  
epoch: 4  
Initial

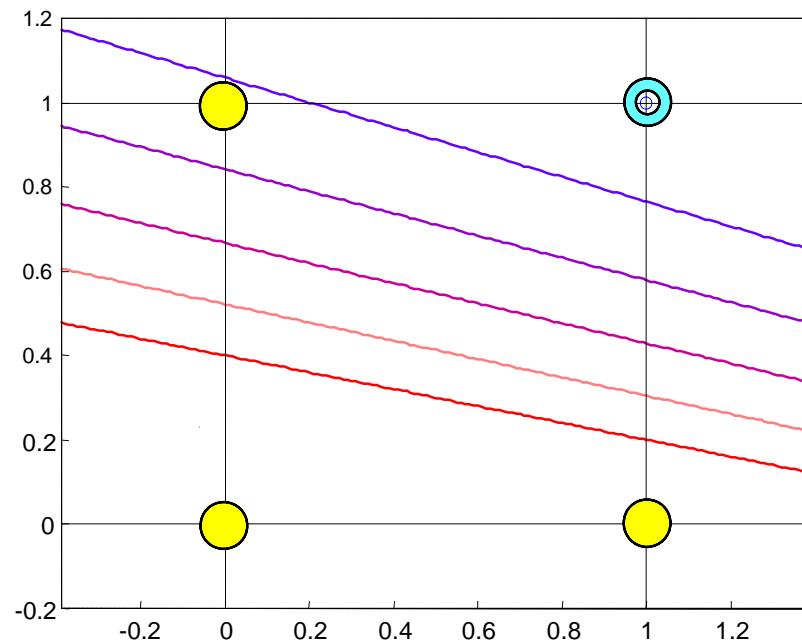
Initial Values

$$w_1 = 0.5$$

$$w_2 = 2.5$$

$$q \text{ (b)} = 1.0$$

$$a = 0.2$$



# Perceptron Learning Rule depends on initial values

$$a^*(t-o)$$

	Perceptron Learning Example: AND Gate							$\sum X_i * W_i$	Bias: Let $X_0 = 1$ , $\text{Alpha} = 0.5$				
	Input			Output				Alpha =		0.5			
	X0	X1	X2	1.0 * W0	X1 * W1	X2 * W2	Total	target	actual	Alpha * (t-o)	W0	W1	W2
											0.1	0.1	0.1
1	1	0	0	0.10	0.00	0.00	0.10	0	1	-0.50	-0.40	0.10	0.10
	1	0	1	-0.40	0.00	0.10	-0.30	0	0	0.00	-0.40	0.10	0.10
	1	1	0	-0.40	0.10	0.00	-0.30	0	0	0.00	-0.40	0.10	0.10
	1	1	1	-0.40	0.10	0.10	-0.20	1	0	0.50	0.10	0.60	0.60
2	1	0	0	0.10	0.00	0.00	0.10	0	1	-0.50	-0.40	0.60	0.60
	1	0	1	-0.40	0.00	0.60	0.20	0	1	-0.50	-0.90	0.60	0.10
	1	1	0	-0.90	0.60	0.00	-0.30	0	0	0.00	-0.90	0.60	0.10
	1	1	1	-0.90	0.60	0.10	-0.20	1	0	0.50	-0.40	1.10	0.60
3	1	0	0	-0.40	0.00	0.00	-0.40	0	0	0.00	-0.40	1.10	0.60
	1	0	1	-0.40	0.00	0.60	0.20	0	1	-0.50	-0.90	1.10	0.10
	1	1	0	-0.90	1.10	0.00	0.20	0	1	-0.50	-1.40	0.60	0.10
	1	1	1	-1.40	0.60	0.10	-0.70	1	0	0.50	-0.90	1.10	0.60

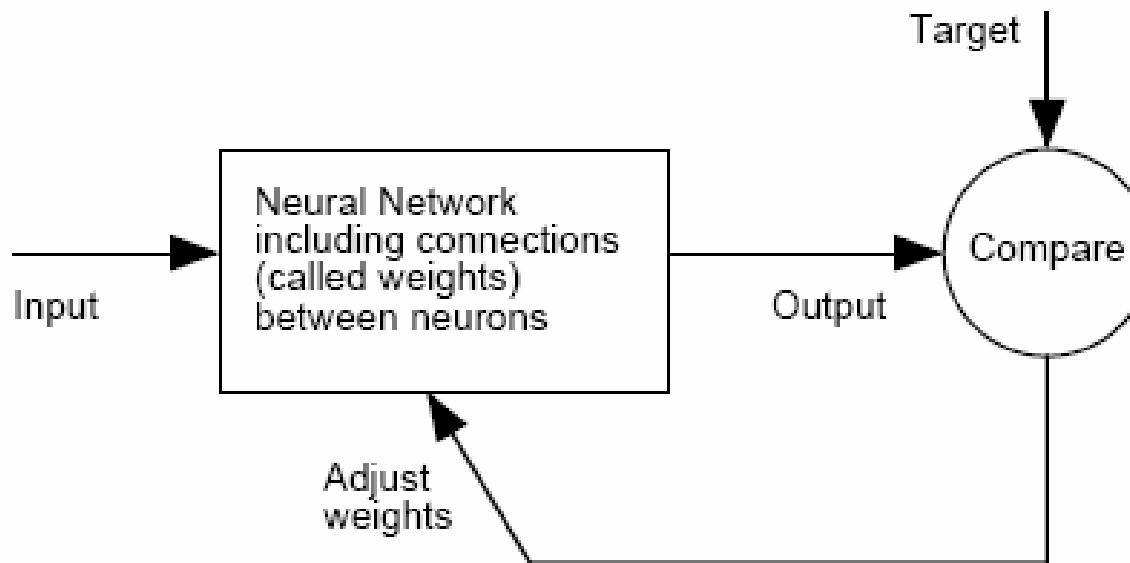
# Perceptron Learning Rule depends on initial values

Input							Output		Alpha =	0.5		
X0	X1	X2	$1.0 * W_0$	$X_1 * W_1$	$X_2 * W_2$	Total	target	actual	$\text{Alpha} * (t-o)$	$W_0$	$W_1$	$W_2$

4	1	0	0	-0.90	0.00	0.00	-0.90	0	0	0.00	-0.90	1.10	0.60
	1	0	1	-0.90	0.00	0.60	-0.30	0	0	0.00	-0.90	1.10	0.60
	1	1	0	-0.90	1.10	0.00	0.20	0	1	-0.50	-1.40	0.60	0.60
	1	1	1	-1.40	0.60	0.60	-0.20	1	0	0.50	-0.90	1.10	1.10
5	1	0	0	-0.90	0.00	0.00	-0.90	0	0	0.00	-0.90	1.10	1.10
	1	0	1	-0.90	0.00	1.10	0.20	0	1	-0.50	-1.40	1.10	0.60
	1	1	0	-1.40	1.10	0.00	-0.30	0	0	0.00	-1.40	1.10	0.60
	1	1	1	-1.40	1.10	0.60	0.30	1	1	0.00	-1.40	1.10	0.60
6	1	0	0	-1.40	0.00	0.00	-1.40	0	0	0.00	-1.40	1.10	0.60
	1	0	1	-1.40	0.00	0.60	-0.80	0	0	0.00	-1.40	1.10	0.60
	1	1	0	-1.40	1.10	0.00	-0.30	0	0	0.00	-1.40	1.10	0.60
	1	1	1	-1.40	1.10	0.60	0.30	1	1	0.00	-1.40	1.10	0.60
7	1	0	0	-1.40	0.00	0.00	-1.40	0	0	0.00	-1.40	1.10	0.60
	1	0	1	-1.40	0.00	0.60	-0.80	0	0	0.00	-1.40	1.10	0.60
	1	1	0	-1.40	1.10	0.00	-0.30	0	0	0.00	-1.40	1.10	0.60
	1	1	1	-1.40	1.10	0.60	0.30	1	1	0.00	-1.40	1.10	0.60

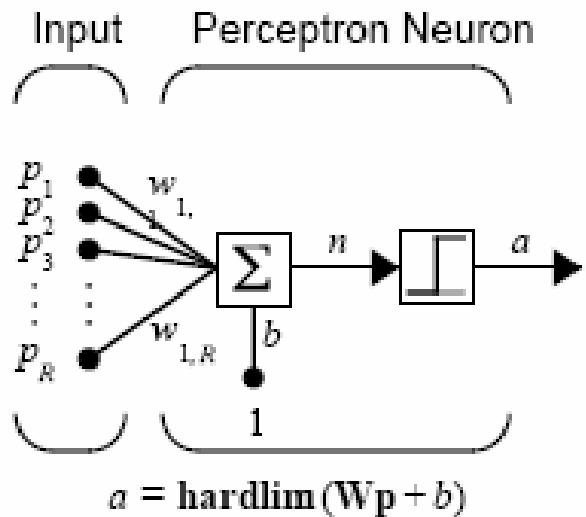
$a * (t - o)$   
isn't change  
apant Ralchaoen, Ph.D.

# Supervised Learning



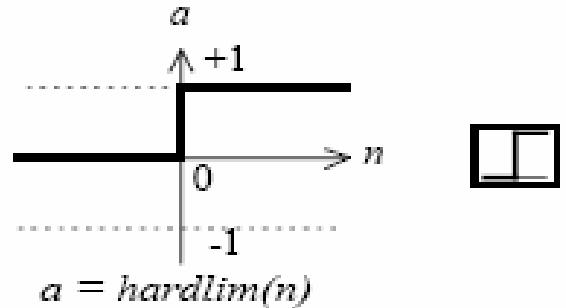
- *Perceptron are learning by adjusting weights !*
- *Feeding Input and Output (target)*
  - *One by one (Online Learning) Perceptron*
  - *All in one (Batch Learning)*

# Perceptron – One Neuron and one layer Model



Where...

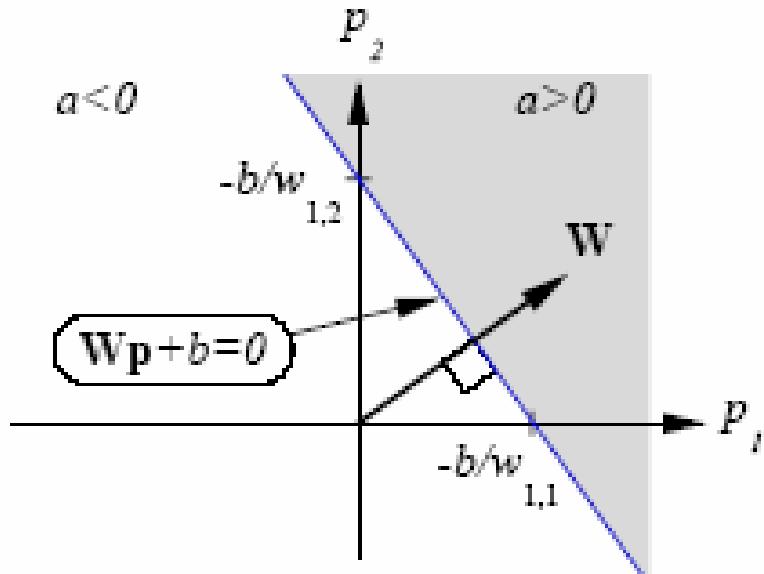
$R$  = number of elements in input vector



Hard-Limit Transfer Function

- $p_1, \dots, p_R$  – input patterns
- $w_1, \dots, w_R$  - synaptic weights
- $w_0 (b)$  - threshold (Bias)
- $f(n)$  - activation function:  $f(n) = \text{hardlim}(n)$
- $a$  - output:  $a = f(n)$

# Perceptron – As decision boundary



Linear equation:

$y = ax + b$ , where  
a is a slop.

$$ax - y + b = 0$$

is equal to

$$w_1 x_1 + w_2 x_2 + b = 0$$

or

$$\mathbf{W}\mathbf{p} + b = 0$$

Two classification regions are formed by the *decision boundary* line  $L$  at  $\mathbf{W}\mathbf{p} + b = 0$ . This line is perpendicular to the weight matrix  $\mathbf{W}$  and shifted according to the bias  $b$ . Input vectors above and to the left of the line  $L$  will result in a net input greater than 0; and therefore, cause the hard-limit neuron to output a 1. Input vectors below and to the right of the line  $L$  cause the neuron to output 0. The dividing line can be oriented and moved anywhere to classify the input space as desired by picking the weight and bias values.

# Perceptron by using MATLAB toolbox

**NEWP** Create a perceptron.

## Syntax

```
net = newp  
net = newp(pr,s,tf,lf)
```

## Description

Perceptrons are used to solve simple (i.e. linearly separable) classification problems.

**PR** - Rx2 matrix of min and max values for R input elements.

**S** - Number of neurons.

**TF** - Transfer function, default = '**hardlim**'.

**LF** - Learning function, default = '**learnp**'.

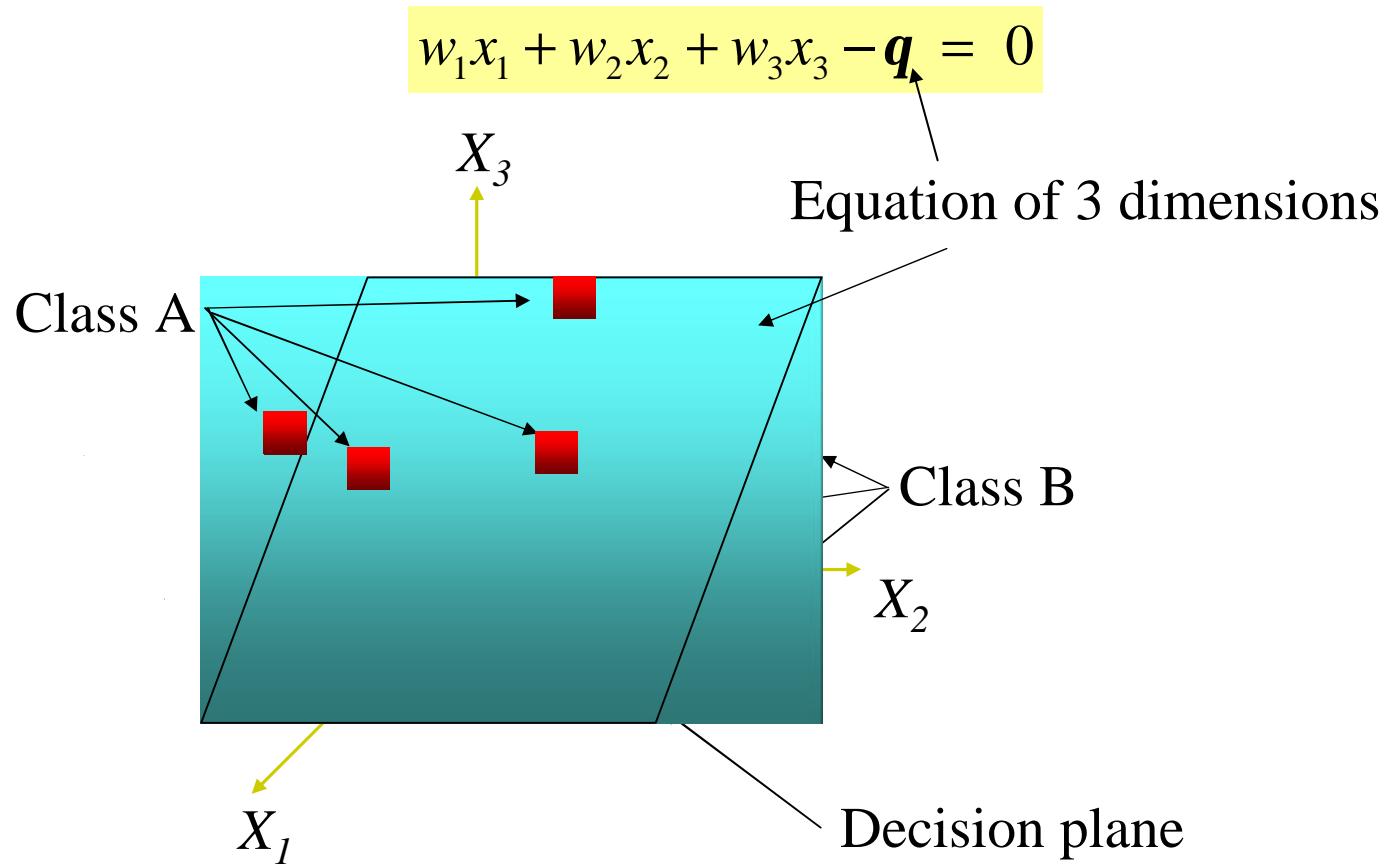
Returns a new perceptron.

# AND Function by using MATLAB toolbox

```
net = newp([0 1; 0 1],1); %This code creates a perceptron layer with one 2-element  
% input (ranges [0 1] and [0 1]) and one neuron.  
% Initial weight [0 0] and bias 0  
  
P = [0 0 1 1; 0 1 0 1]; % And Input patterns  
T = [0 0 0 1]; % Target  
  
net.IW{1} = [1 1] % display weight vector  
net.b{1} = 1 % display bias  
  
net.trainParam.epochs = 2; % train (learn) for a maximum of 2 epochs  
net = train(net,P,T);  
  
a = sim(net,P); % simulate the network's output again (test pattern)  
a = [0 1 1 1] % Result from test pattern
```

# Higher Dimension Feature Space

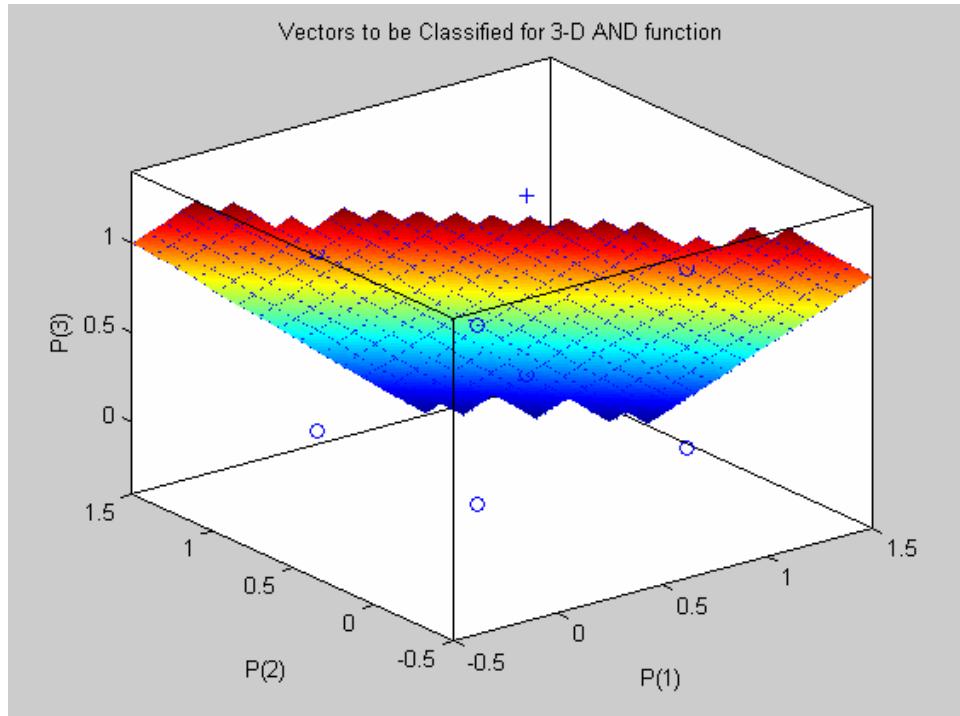
In case of 3 dimensions input data,  
decision function is hyper plane



# 3-D AND Function by using MATLAB toolbox

% 3D perceptron

```
net = newp([0 1; 0 1; 0 1],1);
P = [0 0 0; 0 0 1; 0 1 0; 0 1 1; 1 0 0; 1 0 1; 1 1 0; 1 1 1]'; % AND Function
T = [0; 0; 0; 0; 0; 0; 0; 1]';
% initial weight and bias
net.IW{1} = [1 1 1]; net.b{1} = 0;
% train or learning
net.trainParam.epochs = 1;
net = train(net,P,T);
plotpv(P,T);
plotpc(net.IW{1},net.b{1});
```



# OR Function by using MATLAB

```
net = newp([0 1; 0 1],1); %This code creates a perceptron layer with one 2-element  
% input (ranges [0 1] and [0 1]) and one neuron.  
% Initial weight [0 0] and bias 0  
  
P = [0 0 1 1; 0 1 0 1]; % OR Input patterns  
T = [0 1 1 1]; % Target  
  
net.IW{1} = [1 1] % display weight vector  
net.b{1} = 1 % display bias  
  
net.trainParam.epochs = 2; % train (learn) for a maximum of 2 epochs  
net = train(net,P,T);  
  
a = sim(net,P); % simulate the network's output again (test pattern)  
a = [? ? ? ?] % Result from test pattern
```

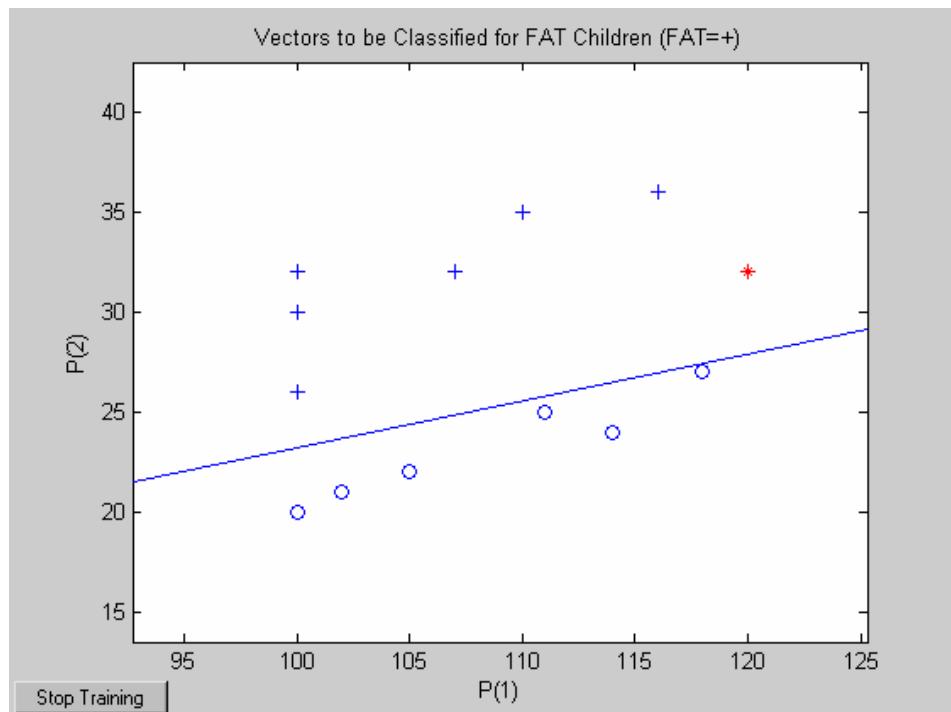
# FAT Children by using MATLAB toolbox

% FAT Children train by perceptron

```
net = newp([90 130; 10 50],1);
P = [100 20; 100 26; 100 30; 100 32; 102 21; 105 22; 107 32; 110 35; 111 25;
      114 24; 116 36; 118 27]'; % Fat Children
T = [0; 1; 1; 1; 0; 1; 1; 0; 0; 1; 0]'; % 1 = fat, 0 = not fat
net.trainParam.epochs = 40;
net = train(net,P,T);
plotpv(P,T);
plotpc(net.IW{1},net.b{1});
```

% FAT Children test a new data (\*)

```
NP = [120 32]';
hold on;
plot(NP(1),NP(2),"r");
Y = sim(net,NP)
```



# Programming in MATLAB Exercise

## ■ Exercise:

1. Write MATLAB to solve the question 3 (OR Function) in **Exercise 3**.
  
2. Write MATLAB to solve the question 4 (FAT Child Problem) in **Exercise 3**.

# Limitation of Perceptron (XOR Function)

No.	P1	P2	Output/Target
1.	0	0	0
2.	0	1	1
3.	1	0	1
4.	1	1	0

